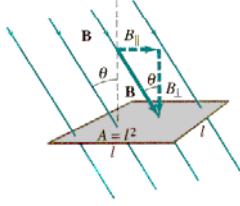


# 4 – Magnetism

## Faraday's Law of Induction

*Magnetic flux defined*

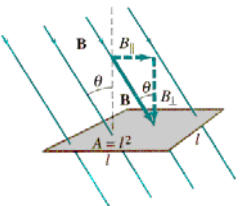


- Quantitative investigation by Faraday yielded
- Magnitude of  $\mathcal{E}$  depends on time
- The more rapid change in Magnetic Field, the higher the  $\mathcal{E}$
- magnetic flux – fluctuation in B;  $\Phi_B$
- $\mathcal{E}$  NOT simply proportional to changing B, BUT rather changing B through a loop of area A

## Faraday's Law of Induction

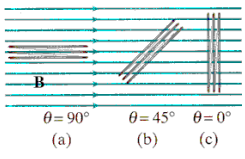
- $\Phi_B = B \perp A = BA \cos(\theta)$
- $B \perp$  is the component B perpendicular to the face of the coil
- $\theta$  is the angle between B and a line drawn  $\perp$  the face of the coil

*Magnetic flux defined*



## Faraday's Law of Induction

**FIGURE 21-4** Magnetic flux  $\Phi_B$  is proportional to the number of lines of **B** that pass through the loop.

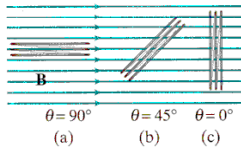


- Given a square coil of side  $\ell$ 
  - $A = \ell^2$
- When the face of the coil is parallel to B,  $\theta = 90^\circ$  and  $\Phi_B = \text{ZERO}$
- When B is perpendicular to coil
  - $\theta = 0^\circ$  and  $\Phi_B = BA$
  - When  $\theta = 0^\circ$ ,  $\Phi_B$  is at a MAXIMUM
- $\Phi_B$  is proportional to total # of lines passing through coil so when  $\theta = 90^\circ$ , no lines pass through the coil therefore the flux is ZERO

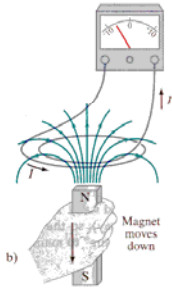
## Faraday's Law of Induction

- $\Phi_B = T \cdot m^2 = \text{Weber} = 1 \text{ Wb} = 1 T \cdot m^2$
- If the flux through N loops of wire changes by an amount  $\Delta\Phi_B$  during a time  $\Delta t$ , the average emf during this time is
- $$\mathcal{E} = -N \frac{\Phi_B}{\Delta t}$$
- Lenz's law**--The negative sign shows direction. An induced emf ALWAYS gives rise to a current whose B opposes the original change in flux.

**FIGURE 21-4** Magnetic flux  $\Phi_B$  is proportional to the number of lines of **B** that pass through the loop.

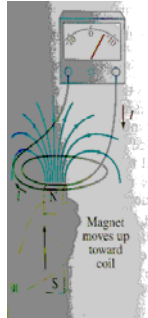


## Lenz's Law



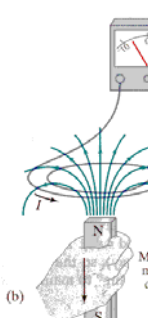
- Move a magnet thru a coil and an emf results therefore a current is produced
- The current produces its own magnetic field

### Lenz's Law



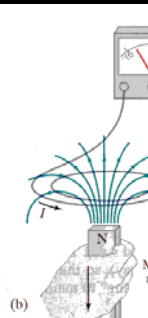
- In a) the distance between the coil and the magnet decreases therefore B and flux through coil increases
- The magnetic field points up while the magnetic field of the induced current points down; opposite to each other!

### Lenz's Law



- Lenz's Law tells us that the current moves as shown in b) [move the magnet down and the current reverses and travels up as indicated by the needle moving to the other side of zero]
- "The flux is decreases so the induced current produces and upward magnetic field that is "trying" to keep equilibrium

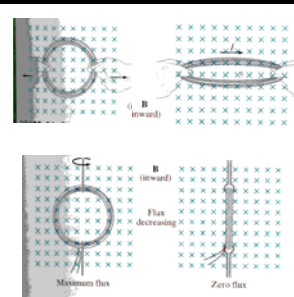
### Lenz's Law



- If Lenz's Law was NOT true: Induced emf produces  $\Phi_B$  in the same direction and current would "grow" to infinity with a power of  $P=I^2R$  and violate the first law of thermodynamics!
- Therefore Lenz's Law is consistent with the first law of thermodynamics

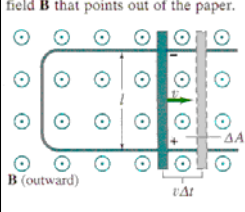
### Lenz's Law

- $\mathcal{E}$  is induced whenever there is a change in flux
  - $\Phi_B = BA \cos(\theta)$
- $\mathcal{E}$  is induced in THREE ways:
  - $\Delta B$
  - $\Delta A$  of loop in field
  - $\Delta$  loops orientation with respect to field



### $\mathcal{E}$ in a Moving Conductor

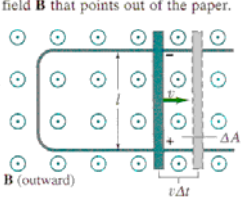
**FIGURE 21-9** A conducting rod is moved to the right on a U-shaped conductor in a uniform magnetic field  $\mathbf{B}$  that points out of the paper.



- Assume a uniform  $\mathbf{B}$  is  $\perp$  to area bounded by the U-shaped conductor and the movable rod resting on it.
- The rod moves at a speed  $v$  travels a distance
  - $\Delta x = v \Delta t$  in a time  $\Delta t$
- Area of loop increases
  - $\Delta A = \ell \Delta x = \ell v \Delta t$
- $E = \frac{\Delta \Phi_B}{\Delta t} = \frac{B \Delta A}{\Delta t} = \frac{B \ell v \Delta t}{\Delta t} = B \ell v$

### $\mathcal{E}$ in a Moving Conductor

**FIGURE 21-9** A conducting rod is moved to the right on a U-shaped conductor in a uniform magnetic field  $\mathbf{B}$  that points out of the paper.



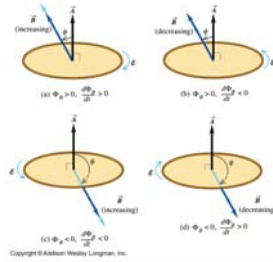
- This works ONLY if  $\mathbf{B}$ ,  $\ell$ ,  $v$  are mutually perpendicular.
- $E = \frac{\Delta \Phi_B}{\Delta t} = \frac{B \Delta A}{\Delta t} = \frac{B \ell v \Delta t}{\Delta t} = B \ell v$
- IF not mutually perpendicular, simply use the perpendicular components (sin, cos)

## $\Delta B$ Produces $\mathcal{E}$

- Electrons in a moving conductor feel a force therefore there is an electric field in a conductor

$$\mathcal{E} = \frac{F}{q} = \frac{qvB}{q} = vB$$

- Move conductor or move magnetic field—you get an emf either way.



*fin.*